

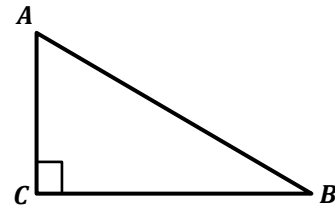
Lesson 5: Criterion for Perpendicularity

Classwork

Opening Exercise

In right triangle ABC , find the missing side.

- a. If $AC = 9$ and $CB = 12$, what is AB ? Explain how you know.



- b. If $AC = 5$ and $AB = 13$, what is CB ?

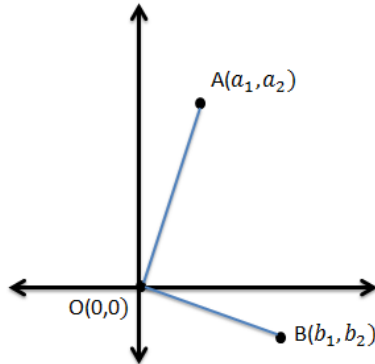
- c. If $AC = CB$ and $AB = 2$, what is AC (and CB)?

Exercise 1

- Use the grid on the right.
 - Plot points $O(0, 0)$, $P(3, -1)$, and $Q(2, 3)$ on the coordinate plane.
 - Determine whether \overline{OP} and \overline{OQ} are perpendicular. Support your findings.



Example 2



Exercises 2–3

2. Given points $O(0,0)$, $A(6,4)$, $B(24, -6)$, $C(1,4)$, $P(2, -3)$, $S(-18, -12)$, $T(-3, -12)$, $U(-8,2)$, and $W(-6,9)$, find all pairs of segments from the list below that are perpendicular. Support your answer.

\overline{OA} , \overline{OB} , \overline{OC} , \overline{OP} , \overline{OS} , \overline{OT} , \overline{OU} , and \overline{OW}

3. The points $O(0,0)$, $A(-4,1)$, $B(-3,5)$, and $C(1,4)$ are the vertices of parallelogram $OABC$. Is this parallelogram a rectangle? Support your answer.



Problem Set

1. Prove using the Pythagorean theorem that \overline{AC} is perpendicular to \overline{AB} given points $A(-2, -2)$, $B(5, -2)$, and $C(-2, 22)$.
2. Using the general formula for perpendicularity of segments through the origin and $(90, 0)$, determine if \overline{OA} and \overline{OB} are perpendicular.
 - a. $A(-3, -4)$, $B(4, 3)$
 - b. $A(8, 9)$, $B(18, -16)$
3. Given points $O(0, 0)$, $S(2, 7)$, and $T(7, -2)$, where \overline{OS} is perpendicular to \overline{OT} , will the images of the segments be perpendicular if the three points O , S , and T are translated four units to the right and eight units up? Explain your answer.
4. In Example 1, we saw that \overline{OA} was perpendicular to \overline{OB} for $O(0, 0)$, $A(6, 4)$, and $B(-2, 3)$. Suppose we are now given the points $P(5, 5)$, $Q(11, 9)$, and $R(3, 8)$. Are segments \overline{PQ} and \overline{PR} perpendicular? Explain without using triangles or the Pythagorean theorem.
5. Challenge: Using what we learned in Exercise 2, given points $C(c_1, c_2)$, $A(a_1, a_2)$, and $B(b_1, b_2)$, what is the general condition of a_1 , a_2 , b_1 , b_2 , c_1 , and c_2 that ensures \overline{CA} and \overline{CB} are perpendicular?
6. A robot that picks up tennis balls is on a straight path from $(8, 6)$ toward a ball at $(-10, -5)$. The robot picks up a ball at $(-10, -5)$ and then turns 90° right. What are the coordinates of a point that the robot can move toward to pick up the last ball?
7. Gerry thinks that the points $(4, 2)$ and $(-1, 4)$ form a line perpendicular to a line with slope 4. Do you agree? Why or why not?